

# The geomagnetic jerk of 2003.5-characterisation with regional observatory secular variation data

Yan Feng<sup>\*1,2</sup>, Richard Holme<sup>3</sup>, Grace Alexandra Cox<sup>3</sup>, Yi Jiang<sup>1</sup>

1. *The College of Mathematics and Statistics, Nanjing University of Information Science & Technology, 219, Ningliu Road, 210044, Nanjing, China.*

*Email: frank\_feng8848@163.com*

2. *State Key Laboratory of Space Weather, Chinese Academy of Sciences, 100080, Beijing, China.*

3. *School of Environmental Sciences, University of Liverpool, L69 3GP, Liverpool, UK.*

---

## Abstract

The 2003.5 geomagnetic jerk was identified in geomagnetic records from satellite data, and a matching feature reported in variations in length-of-day ( $\Delta\text{LOD}$ ), but detailed study has been hampered by lack of geomagnetic observatory data where it appears strongest. Here we examine secular variation (annual differences of monthly means) based on a new resource of 43 Chinese observatory records for 1998 until the present, focusing on 10 series of particularly high quality and consistency. To obtain a clean series, we calculate the covariance matrix of residuals between measurements and a state-of-the-art field model, CHAOS-6, and use eigenvalue analysis to remove noisy contributions from the uncorrected data. The magnitude of the most significant eigenvector correlates well with  $\text{Dcx}$  (corrected, extended Dst), suggesting the noise originates from unmodelled external magnetic field. Removal of this noise eliminates much coherent misfit around 2003—2005; nevertheless, the 2003.5 jerk is seen clearly in the first time derivative of the East component in Chinese data, and is also seen in the first time derivative of the

vertical component in European data. Estimates of the jerk time are centred on 2003.5, but with some spatial variation; this variation can be eliminated if we allow a discontinuity in the secular variation as well as its temporal gradient. Both regions also provide evidence for a jerk around 2014, although less clearly than 2003.5. We create a new field model based on new data and CHAOS-6 to further examine the regional signals. The new model is close to CHAOS-6, but better fits Chinese data, although modelling also identifies some data features as unphysical.

*Keywords:* Geomagnetic field, Secular variation, Jerk, CHAOS-6, Length of day

*PACS:* 91, 25, Le

---

## 1. Background

The observed geomagnetic field originates from field sources both internal and external to the Earth, varying on time scales of milliseconds to billions of years. Largely, short time scales (a year or less) are the result of external variations (changes in the magnetosphere or ionosphere associated with solar field variations), while variations on longer time scales originate from the internal field generated in the Earth's core by the magnetohydrodynamic dynamo. The shortest observed changes that have been attributed to internal variations are the so-called geomagnetic jerks, first defined by Courtillot et al. (1978) as a sudden change in the slope of the geomagnetic secular variation (SV, the first time derivative of the Earth's magnetic field), or equivalently an abrupt (step-like) change in the secular acceleration (SA, the second time derivative). The most widely discussed jerk is in 1969 (Malin and

14 Hodder, 1982), but many others have been identified (e.g., 1978, 1991, 1999  
 15 and 2003) in time series of geomagnetic observatory data, or geomagnetic  
 16 models (Mandea et al., 2010), most recently from 2011 (Chulliat and Maus,  
 17 2014) and 2014 (Torta et al., 2015). A feature of recent interest has been an  
 18 approximately 6-year cycle in SV linking to jerks (Chulliat and Maus, 2014),  
 19 and also seen strongly in variations in Earth rotation (length-of-day, LOD)  
 20 (Gillet et al., 2010; Holme and De Viron, 2013). These observations support  
 21 an association with possible torsional oscillations in the outer core (Bloxham  
 22 et al., 2002), linked to either inner-core rotation and coupling (Mound and  
 23 Buffett, 2003) or an intrinsic flow mode (Gillet et al., 2010). However, there  
 24 remains considerable debate as to the nature of jerks . Are they a global or  
 25 localised feature (Mandea et al., 2010; Torta et al., 2015)? Is the discontinu-  
 26 ity in the second derivative the best way to characterise them (Alexandrescu  
 27 et al., 1996)? Do external field features (Alldredge, 1984; Demetrescu and  
 28 Dobrica, 2014) cause or contribute to some jerks? Are all jerks similar, or  
 29 are there a variety of different types, and potentially causes (Mandea et al.,  
 30 2010)?

31 Most studies on geomagnetic jerks focus on magnetic observatory data,  
 32 because of their long-time stability, and high temporal resolution to define the  
 33 secular variation. However, (Mandea and Olsen, 2006) developed a comple-  
 34 mentary study tool deriving “virtual observatories” using data from magnetic  
 35 satellites, by stacking the data in time for a limited geographical region. The  
 36 derived individual secular variation estimates are of lower quality than those  
 37 from ground based observatories, but provide global data availability rather  
 38 than depending on the sparse and uneven geomagnetic observatory network.

39 Using this method, Olsen and Manda (2007) identified several jerks, includ-  
 40 ing one centred on 2003.5. This feature is of particular interest because it is  
 41 not aligned with the approximately 6-year variation, but nevertheless corre-  
 42 lates with a jerk-like feature in variations in Earth rotation or length of day  
 43  $\Delta\text{LOD}$  (Holme and De Viron, 2013), also separate from the 6-year variation.  
 44 Inference from the rotational record suggests a possible discontinuity in not  
 45 just the rate of secular variation, but the secular variation itself, changing the  
 46 range of possible physical mechanisms that could give rise to it. The similar-  
 47 ity in timing of the two records also constrains other geophysical properties,  
 48 particularly deep-mantle electrical conductivity (Holme and De Viron, 2013).  
 49 To better examine this feature in the geomagnetic data, a study of ground  
 50 observatory data is clearly highly advantageous. Brown et al. (2013) provide  
 51 such a study, but Olsen and Manda (2007) localise the event as around the  
 52  $90^\circ$  E meridian, a geographic region for which easily available data from world  
 53 geomagnetic data centre holdings are sparse. Here we investigate previously  
 54 unutilised data from 43 Chinese observatories covering the period 1998 to  
 55 2016. These data provide a particular tool for studying this jerk, but also a  
 56 potential homogeneous database for future high resolution regional studies  
 57 of secular variation, to compare with other densely instrumented areas such  
 58 as Europe. We compare these data with the European data, focusing partic-  
 59 ularly on the 2003.5 jerk to determine whether there exist linked changes in  
 60 Asia and Europe, which therefore could provide a global constraint on secular  
 61 variation, and a direct observational constraint on the rapid variation of the  
 62 geodynamo. We characterize the short-period variation in the time series as  
 63 being related to external field, and by subtracting this influence, strengthen

64 the interpretation and better constrain the timing of the 2003.5 jerk. To  
65 explore the content of the new data, we create a new global, time-dependent  
66 model which is both close to the field predicted by the CHAOS-6 model and  
67 also better fits the newly available Chinese data. We will use this tool to  
68 better characterize all rapid variations in secular variation.

69

## 70 2. Data

71 There are currently 43 operational Chinese observatories (Figure 1) pro-  
72 viding good spatial coverage throughout the Chinese mainland, with records  
73 broadly available from 1998 to the present day, and many extending earlier.  
74 Available observatories were established and are maintained by the Geo-  
75 magnetic Network of China, Chinese Earthquake Administration, which has  
76 provided hourly mean data; many of these data are not as yet held by the  
77 World Data Centers. To compare with and verify our results, 7 European  
78 observatories (figure 2) are also studied. The codes of all 43 Chinese obser-  
79 vatories are listed in the appendix.

80

Figure 1

Figure 2

81 As we are interested primarily in internal field variations, from all avail-  
82 able hourly data we calculated monthly means of the three components  
83 (northward  $X$ , eastward  $Y$  and vertically downward  $Z$ ) of the magnetic field  
84 of each observatory, thereby eliminating high-frequency external variations.  
85 We estimated SV determining annual differences of monthly means, for ex-

ample for  $Y$  as:

$$\left. \frac{dY}{dt} \right|_t = Y_{(t+6)} - Y_{(t-6)} \quad (1)$$

where  $t$  denotes time in months. By taking differences, we eliminate constant crustal field offsets (Bloxham and Jackson, 1992). By taking annual differences, we reduce the influence of external noise, e.g. magnetospheric ring currents, particularly those components with annual cycles. This method is equivalent to the approach of Mandeia et al. (2000), who took monthly differences, but then applied a 12-month running mean. There are generally two problems when dealing with the data: baseline jumps (or erroneous data) and data gaps, resulting from many possible causes (e.g., instrument error, power failure, station relocation, anthropogenic current disturbance, etc). We have applied all documented baseline corrections, and have identified and corrected for some additional jumps (see appendix). Data gaps are more difficult, and unfortunately many of the Chinese data series are discontinuous. Brown et al. (2013) treated a gap shorter than 6 months by interpolating, while if longer than 6 months the data were split into separate time series. We choose to use the data “as is”, and will consider data gaps by comparison with the CHAOS-6 field model and covariance modelling, described below. Our primary focus is on 10 Chinese observatories with the most continuous records (THJ, JIH, QIX, GLM, TSY, COM, YON, WMQ, DLG and CHL, see figure 1). To compare the results, monthly mean data of 7 European observatories (BEL, CLF, DOU, FUR, HLP, HRB and NGK, see figure 2) are adopted from the Bureau Central de Magntisme Terrestre (BCMT), World Monthly Means Database Project, which provides monthly

averages of components  $dX/dt$ ,  $dY/dt$  and  $dZ/dt$  at 118 observatories world-wide) calculated from hourly means held by the World Data Centre (WDC) for Geomagnetism at the British Geological Survey, Edinburgh (Chulliat and Telali, 2007).

### 3. Jerk-like features

In figures 3-5, we plot the secular variation estimates for both arrays of observatories. For the  $dZ/dt$  component, the plot of variation for the Chinese data is dominated by a linear secular trend. To bring out the rapid changes, we provide an subfigure (middle figure of fig 5) in which this trend is removed.

Figure 3

Figure 4

Figure 5

For  $dX/dt$ , the rapid variation shows strong correlation (correlation coefficient  $r=0.77$ ) between China and Europe, with many oscillations in common during 1998-2015. Focusing on 2003.5 and 2014, changes in slope ( $\vee$  and  $\wedge$  shapes) are present simultaneously in both data sets. For  $dY/dt$ , a longer term  $\vee$  shape also can be clearly recognized in 2003.5 in China, but not clearly in 2014. In contrast, European data express clear jerk like shape in 2014 but not in 2003.5. For  $dZ/dt$ , comparing the detrended Chinese data we find good agreement between two regions around 2003.5 ( $r=0.91$ ) and 2014 ( $r=0.83$ ). To summarise, 2003.5's jerk could be clearly identified in China among  $dX/dt$ ,  $dY/dt$  and  $dZ/dt$ , consistent with Olsen and Mande (2007), and 2014's jerk can be located as Torta et al. (2015). 2014's jerk can also be distinguished in Australia, central Pacific and Europe through models

including CHAOS-6 (Finlay et al., 2016; Brown et al., 2016). To other jerks (Mandea et al., 2010), 1999 and 2011’s jerks can be found in  $dX/dt$  in two regions. It is easy to find 2009’s jerk in  $dY/dt$  and  $dZ/dt$  in Europe but not in China. Finally, a jerk-like feature may be emerging around 2015.

#### 4. External fields

The data contain a strong component that is related to external and induced fields, in particular from the large-scale magnetospheric ring currents and associated induced signals due to ground electrical conductivity. Strong correlation between variations of different components (particularly  $dX/dt$  and  $dZ/dt$ ) are particularly indicative of this. Magnetic field models such as CHAOS-6 and CM4 (Finlay et al., 2016; Sabaka et al., 2004) are constructed to co-estimate the external field, with some allowance for the induced field. This external effect is parameterized by an a priori geomagnetic index, e.g. RC or Dst. However, the global model of the ring current does not include the influence of possible local conductivity structure on induced fields. As an alternative, Wardinski and Holme (2006) showed that the residual between observation and model can replace the Dst index in their calculations as a proxy for unmodelled external signals. Removal of such signals substantially reduces the standard deviation of the data, therefore improving the resolution of internal features such as jerks (Brown et al., 2013).

We follow Wardinski and Holme (2006) to create the covariance matrix of residuals of observatory monthly mean annual differences and CHAOS-6 model secular variation prediction. We assume that the residuals are zero-



156 mean, so we can define the elements of the covariance matrix

$$cov(p, q) = \frac{\sum_{i=1}^n P_i Q_i}{n}, \quad (2)$$

157 where  $P$ ,  $Q$  are residuals of the secular variation estimates of particular  
 158 components from one or two observatories, with the sum over  $n$  observations.  
 159 For  $n$  observatories each with 3 component data  $dX/dt$ ,  $dY/dt$  and  $dZ/dt$ ,  
 160 the covariance matrix is of order  $3n$ ; the eigenvalues and eigenvectors of the  
 161 matrix are then determined. We calculate the covariance matrices separately  
 162 for groups of 10 Chinese and 7 European sites, yielding 30 and 21 eigenvalues,  
 163 respectively, plotted in figure 6.

Figure 6

164 In both data sets, there is a clear sharp decrease between the first and  
 165 second eigenvalues, after which the values decrease gradually. As a result,  
 166 the first eigenvector makes a dominant contribution to the misfit. In figure 7,  
 167 we plot the contributions to this eigenvector for the 10 Chinese observatories.

Figure 7

168 The spatial structure of this eigenvector is indicative of its origin from  
 169 the ring current, which produces a field dominantly in  $dX/dt$  and  $dZ/dt$   
 170 directions, with the relative values depending on the observatory's location.  
 171 Here,  $dX/dt$  dominates because the Chinese observatories are at low mag-  
 172 netic latitude. The quietest component as seen in this figure is  $dY/dt$ , which  
 173 is perpendicular to the ring current field (Pinheiro et al., 2011). Note that  
 174 we did not initially obtain this result, but instead determined an eigenvector  
 175 dominated by one particular observatory; this turned out to be an unmod-  
 176 elled baseline shift, and the ring current structure only became clear when  
 177 such data artefacts were removed. As a result, the method also acts as a

178 sensitive test of data quality.

179 We examine the spatial structure of this noisiest (largest eigenvalue)  
180 eigenvector in more detail in Figure 8. For the 10 observatories already  
181 considered, we extracted the ( $dX/dt$ ,  $dY/dt$ ,  $dZ/dt$ ) components for each  
182 observatory, and normalized each 3 vector to unit length. The other 33 ob-  
183 servatories have data of lower quality; to consider these observatories as well,  
184 we repeat the covariance/eigenanalysis by adding one of those observato-  
185 ries to the 10 good observatories sequentially (making each eigenanalysis of  
186 11 observatories (33 data series)), and each time calculated the normalized  
187 components for the additional observatory. We plot the  $dX/dt$  and  $dY/dt$   
188 components; an observatory with only a  $dZ/dt$  component would plot at the  
189 origin.

Figure 8

190 The more consistent the data series for different observatories, the closer  
191 the points for the different observatories should be. In figure 8, the left  
192 hand figure shows broad consistency between the observatories. The right  
193 hand figure provides more details, with 8 observatories separated from the  
194 majority; examining the series shows that they contain large misfits likely  
195 resulting from uncorrected artefacts. For the 35 consistent series, many have  
196 large data gaps, leading to our decision to concentrate analysis on only 10  
197 good observatories with broadly continuous records.

198 To support our hypothesis that this largest noise source is related to the  
199 ring current, we compare the component of this eigenvector in the residuals  
200 at each time (the dot product of the residual vector with this unit eigenvec-  
201 tor) with an index of ring-current activity. We use an corrected, extended

202 Dst index, Dcx, which is achieved selecting 17 stations and correcting for  
 203 the quiet-time seasonal variation (Mursula et al., 2008). (The index is provi-  
 204 sional from non-definitive data for 14 stations for 2012-2016.) We calculate  
 205 the annual differences of Dcx and compared to the noisy contributions from  
 206 Chinese and European observations (figure 9).

Figure 9

207 Figure 9 shows a good agreement between the annual differences in vari-  
 208 ations of Dcx and noisy contributions from both China and Europe, par-  
 209 ticularly in the active periods 2003-2006 and 2014 onwards, when Dcx sig-  
 210 nificantly oscillates and their trends look highly consistent. This situation  
 211 implies that the jerk signature around 2003.5 and 2014 could be seriously  
 212 influenced by external fields. The correlation coefficient between Chinese  
 213 magnetic observatories and Dcx is 0.70, and that between European obser-  
 214 vatories and Dcx is 0.68. Note also that the eigenvectors for the separate  
 215 analyses for China and Europe have correlation coefficient 0.96, confirming  
 216 the conjecture of Wardinski and Holme (2011) that the dominant eigenvector  
 217 and its magnitude may be a better correction method than scaling with Dcx.

## 218 5. Cleaned data

219 We have shown that the largest eigenvalue/eigenvector of the misfit of the  
 220 data to the field model is not random, but arises from a specific source, likely  
 221 dominated by variations in the magnetospheric ring current. Therefore, to  
 222 clean the data for better analysis of possible internal signals, we remove the  
 223 contribution of the highest (noisiest) eigenvalue, which we believe strongly  
 224 reduces the influence of magnetospheric ring-current variation. We subtract

225 the noisy contributions corresponding to the largest eigenvalue/eigenvector  
 226 as follows:

$$\mathbf{r}' = \mathbf{r} - (\mathbf{r} \cdot \mathbf{v})\mathbf{v}, \quad (3)$$

227 where  $\mathbf{r}$  is residual vectors at a particular time,  $\mathbf{v}$  is the unit normalized  
 228 eigenvectors corresponding to the largest eigenvalue. The clean (denoised)  
 229 data have the influence of the largest eigenvalue removed, plotted in Figures  
 230 10-12.

Figure 10

Figure 11

Figure 12

231 Much of the apparent jerk signal is eliminated, suggesting that much  
 232 of the sharp change in  $dX/dt$  and  $dZ/dt$  around 2003.5 is of external ori-  
 233 gin, especially from the magnetospheric ring current. This is of particular  
 234 significance, as the original identification of the jerk by Olsen and Manda  
 235 (2007) was from analysis of the  $dZ/dt$ , which might therefore also have been  
 236 contaminated by external field structure. The similar timings also support  
 237 and explain earlier discussions of jerk signals from in part external sources  
 238 (Alldredge, 1984; Demetrescu and Dobrica, 2014). Comparing with figure 7,  
 239  $dX/dt$  is most changed with  $dZ/dt$  less;  $dY/dt$  is little changed. In figure  
 240 10,  $dX/dt$  is much changed with fewer oscillations both in China and Europe  
 241 compared with uncorrected variation. The 2014 jerk can be roughly distin-  
 242 guished while 2003.5 is not clear. Figure 11 shows little change in  $dY/dt$   
 243 due to this direction being perpendicular to the magnetic field of the ring  
 244 current; the 2003.5 jerk can still be clearly identified in China. For  $dZ/dt$ ,  
 245 we again linearly detrend the Chinese data for clarity. No clear jerk is seen

246 in the Chinese data, but a jerk signal remains in the European data.

247 To highlight the suggested jerks, we replot the figures for  $dY/dt$  for China  
248 (Figure 13) and  $dZ/dt$  for Europe (Figure 14).

Figure 13

Figure 14

249 A jerk is present in both regions at around 2003.5, both records show  
250 some evidence of a jerk in 2014, and overall the two signals show broad anti-  
251 correlation throughout the interval. Therefore the two jerks are global sig-  
252 nals, albeit seen most clearly in different components in different geographic  
253 regions, and therefore in a field model will be dominated by spherical har-  
254 monic field components of low degree. We further examined the SV of the  
255 33 less good Chinese observatories in 2003.5 and 2014 in the same way; these  
256 two jerks are reflected particularly cleanly at 18 and 6 of these observatories  
257 respectively, where the limited numbers are due to lack of data rather than  
258 evidence that the jerk is *not* present.

259 Finally, we estimate the time of the 2003.5 jerk in the Chinese data. We  
260 determine best fit lines for the data before and after the jerk, and calculate  
261 the time of their intersection, as a classical measure of jerk timing. The  
262 results are presented in Table 1.

Table 1

263 The mean timing is close to 2003.5, although it is not possible to state  
264 that the jerk is simultaneous at all locations. However, this time also assumes  
265 that SV is continuous. Evidence from both  $\Delta\text{LOD}$  and wavelet analysis of  
266 secular variation data (Alexandrescu et al., 1996) suggests that a jerk might  
267 involve a change not only in secular variation gradient, but also in its value.

Such a jump would be smoothed by the analysis: an annual first difference (as used to estimate the secular variation) is equivalent to a 12-month running average of secular variation, smoothing any such jump. To investigate this, we define the jerk time to be 2003.5, allowing a discontinuity in SV, and take a running average. Figure 15 provides an example for the observatory GLM. In all cases, the prediction provides an equally good fit to the data as allowing a difference in calculation of the jerk time, and as here the running averages are almost indistinguishable. We therefore claim that the data are consistent with both a variation in jerk timing over China, but also with a jerk at a common time but allowing an offset in secular variation, and may not allow these two hypotheses to be distinguished.

Figure 15

## 6. A perturbed field model

To this point, we have taken the CHAOS-6 model as a true representation of the field for the Chinese region, despite that model not being constrained by the new secular variation data. Some features in SV not predicted by CHAOS-6 seem coherent between several (although by no means all) of the different data series. To investigate the possible implications of these data, we seek a new global, time-dependent model which is both close to the field predicted by the CHAOS-6 model (and so assumed to match well the satellite data from which it is constructed) and also better fits the newly available Chinese data. Our methodology follows that of Lodge and Holme (2009). We expand in a spherical harmonic basis in latitude and longitude, truncated at spherical harmonic degree  $l_{max} = 14$ , with each coefficient further expanded

291 on a basis of cubic B-splines, with temporarily dense knots at spacing 0.1  
 292 years. The CHAOS6 model is expanded on order 6 B-splines with half-year  
 293 knot spacing; we obtain a reference model from a least-squares fit to each set  
 294 of spline coefficients for each Gauss coefficient; the lower degree of the splines  
 295 is countered by the higher knot density. We seek a model between times  $t_0$   
 296 and  $t_1$  (1997.1 and 2018.1 to match the limits of the CHAOS6 model) min-  
 297 imizing three properties: 1) the mean square misfit to the secular variation  
 298 estimates derived from the 43 Chinese observatories; 2) the time integrated  
 299 square vector misfit at Earth's surface to the CHAOS-6 model; and 3) the  
 300 time integrated squared secular acceleration at the core-mantle boundary  
 301 (CMB). Condition 1 requires a fit to the new data presented here, condition  
 302 2 provides a proxy to the fit to the satellite and observatory data from which  
 303 CHAOS-6 was constructed (defined at Earth's surface), and condition 3 pre-  
 304 vents unreasonably large temporal variation. Condition 1 is implemented  
 305 as a fit to data, while conditions 2 and 3 are both "damping", giving the  
 306 objective function  $\Gamma$  to be minimized as

$$\begin{aligned}
 \Gamma = & \sum_{i=1}^n \left( \dot{\mathbf{B}}(\mathbf{x}_i) - \dot{\mathbf{B}}_i \right)^2 \\
 & + \lambda \int_{t_0}^{t_1} \sum_{l=1}^{l_{max}} (l+1) \sum_{m=0}^l \left( (g_l^m - g_{l \text{ CHAOS}}^m)^2 + (h_l^m - h_{l \text{ CHAOS}}^m)^2 \right) dt \\
 & + \mu \int_{t_0}^{t_1} \sum_{l=1}^{l_{max}} (l+1) \left( \frac{a}{c} \right)^{(2l+4)} \sum_{m=0}^l \left( (\ddot{g}_l^m)^2 + (\ddot{h}_l^m)^2 \right) dt
 \end{aligned} \tag{4}$$

307 The first term is the mean square fit to the secular variation data by the  
 308 model.  $\dot{\mathbf{B}}_i$  is a vector of SV data, with the difference taken to the model  
 309 prediction at observatory location  $\mathbf{x}_i$ . The second term minimizes the mean

310 square misfit mean field integrated over Earth’s surface, radius  $a$ , given by  
 311 the squared difference between the model Gauss coefficients  $g_l^m, h_l^m$  of degree  
 312  $l$  and order  $m$  and those of the CHAOS-6 model. The third term minimises  
 313 the mean square secular acceleration at the core-mantle boundary, radius  $c$ .  
 314 The two damping parameters  $\lambda$  and  $\mu$  allow a range of possible solutions;  
 315 we present three representative possible models, which we designate as low,  
 316 medium and high damping. The low damping allows comparatively large  
 317 secular acceleration, while the high damping provides a model closely con-  
 318 strained to match the field prediction of CHAOS-6. To illustrate the fit to  
 319 the data, we plot the fit for each component to the station YON.

Figure 16

Figure 17

Figure 18

320 The high damping model provides little departure from CHAOS-6; to  
 321 obtain a closer fit to the data, more time variation is required see for example  
 322 Figure 16 ( $dX/dt$ ). That this variation may be unreasonably high is shown  
 323 by a more detailed plot of the  $dZ/dt$  for 2010—2012 (see more details in  
 324 figure 19). The high damped model shows little change to CHAOS-6, while  
 325 the intermediate and low damping models have changed to fit sharp changes  
 326 in the data in 2011.3 which may well be an artifact. Only with low damping  
 327 is the data fit substantially improved; compared to CHAOS-6, the misfit is  
 328 reduced by 22.0%, 18.7% and 22.1% for  $dX/dt$ ,  $dY/dt$ ,  $dZ/dt$  components  
 329 respectively. Even with this weakly damped model, some strong features in  
 330 the data coherent between different observatories are not fit, even when the  
 331 error estimate for a short period (e.g., 2002—2005) is artificially reduced.



332 This implies that such features cannot be represented by the components  
 333 of a potential field are not likely to be a result of unmodelled internal field  
 334 structure, suggesting further cleaning or selection of data to be necessary.

Figure 19

335 The increased temporal structure of the new models is demonstrated by  
 336 considering the secular variation spectrum

$$W'(l, c) = (l + 1) \left(\frac{a}{c}\right)^{(2l+4)} \sum_{m=0}^l (\dot{g}_l^m)^2 + (\dot{h}_l^m)^2, \quad (5)$$

337 Here  $\dot{g}_l^m, \dot{h}_l^m$  are time derivatives of the Gauss coefficients. In Figure 20, we  
 338 show the power spectra at 2004.0 for our three differently damped models,  
 339 also plotting  $W(l, c)/(l(l + 1))$ , which following McLeod (1996) and Holme  
 340 et al. (2011), we might expect to be broadly independent of degree  $l$ .

Figure 20

341 Both the medium and low damping models show a strong rise in secular  
 342 variation power above degree 10, which is unlikely to be physical. In Figure  
 343 21 we compare contour maps of SV at Earth’s surface for CHAOS-6 and  
 344 the weakly damped new model; the broad structure is unchanged, but the  
 345 contours show small scale variations that are probably not justified.

Figure 21

346 A change in SV near China (better matching the data) is achieved, but  
 347 only at the expense of considerably increased detail over the whole globe,  
 348 which is not consistent with the original data. If plotted at the CMB, the  
 349 map of the new model shows excessive small scale structure. We conclude  
 350 that there is no strong evidence in the new data requiring substantial adjust-  
 351 ment to the CHAOS-6 model – substantially improved fit to data requires

unreasonably large small-scale secular variation.

## 7. Discussion and Conclusions

We have examined collections of spatially close geomagnetic observatory records, focusing on a new set of data from Chinese observatories, and for comparison, a set of well-studied European observatories. The Chinese data are of slightly lower quality than the European data: the data are more gappy, and require correction of undocumented baseline jumps. Nevertheless, after such corrections, the data are of high quality, and provide a close to homogenous data set for study of regional intra-decadal and longer secular variation. We have focused on one period in particular, centered around 2003.5, for which a rapid SV change (a geomagnetic jerk) had previously been reported (Olsen and Manda, 2007). This previous identification had been based on a model constructed from satellite data using virtual observatories (averages of satellite data over a limited region); secular variation studies with observatory data will be more robust. Our data show strong features around 2003.5, particularly in the  $dX/dt$  and  $dZ/dt$  components for both the Chinese and European observatory arrays. However, further analysis suggests that these features result from external field variation, probably a jump in the strength of the ring current (reflected in  $D_{cx}$ ). Removing these external fields removes much of the sharp signal in  $dX/dt$  and  $dZ/dt$ , but a clear jerk remains in the  $dY/dt$  component at Chinese observatories. The jerk is also seen in  $dZ/dt$  at European observatories, although some contamination from external sources may remain. Nevertheless, as the features form part of the long term trends in secular variation, we argue that there is a

376 component of internal origin.

377 Using CHAOS-6, we plot the evolution of  $dY/dt$ , and estimates of its  
378 first (SV) and second (SA) derivatives. The broad structure is similar for all  
379 Chinese observatories; we plot QIX, located in the middle of the observatory  
380 grouping, along with its CHAOS-6 predictions.

### Figure 22

381 Figure 22 shows clearly the jerk in the SV around 2003.5, and allowing  
382 for the averaging of the data the SA record is consistent with a jump, per-  
383 haps overly smoothed in the CHAOS-6 model prediction. This figure does  
384 not illustrate evidence in the Chinese data of the most recently identified ge-  
385 omagnetic jerk in 2014 (Torta et al., 2015), this feature is only seen strongly  
386 in 6 Chinese observatories (THJ, GLM, WMQ, CDP, QGZ and HZC).

387 The exact timing of the jerk is of great interest (e.g. Pinheiro et al.  
388 (2011)); time delays have been used to propose higher electrical conductivity  
389 of the deep mantle under certain geographic regions, particularly in the Pa-  
390 cific. Taking the usual definition of a jerk implying continuous SV, both data  
391 and model suggest that even in the limited region covered by the Chinese  
392 data, there is some offset of jerk times with locations. All observatories show  
393 the jerk at around 2003.5, but varying between 2003 (at WMQ, the most  
394 westerly located of our 10 selected observatories) and close to 2004 (DLG,  
395 the most easterly of our observatories). The shift in jerk timing may instead  
396 result from different SV time gradients before and after 2003.5; the jerk is  
397 apparently shifted towards the less steep trending time. This is consistent  
398 with the observations above for WMQ and DLG. However, this simple anal-  
399 ysis is complicated by the possibility of a jump in the secular variation itself,

400 as suggested by the  $\Delta$ LOD data (Holme and De Viron, 2013), but also by  
 401 wavelet studies suggesting that the jerks are not exact jumps in the second  
 402 derivative (Alexandrescu et al., 1996). When the effective 12 month averag-  
 403 ing from taking annual differences of the data is allowed for, the predictions  
 404 assuming continuous SV but varying jerk times, or a common time but dis-  
 405 continuous SV are indistinguishable. Furthermore, the data are still noisy,  
 406 with features that cannot be well-fit by a model of the internal geomagnetic  
 407 field, even after the removal of the largest noise eigenvector, making direct  
 408 analysis of the data difficult. Further study is necessary, particularly focus-  
 409 ing on the sources of the data, but we may conclude at least that the newly  
 410 available Chinese data are consistent with a common time for the jerk of  
 411 around 2003.5.

412 We believe our analysis shows evidence of the 2003.5 jerk appearing at  
 413 widely spaced locations on the Earth, and so that the jerk is of global sig-  
 414 nificance. The timing of the jerk (from the  $dY/dt$  in the Chinese data) is  
 415 also consistent with the feature at 2003.5 reported in the variation in LOD  
 416 (Holme and De Viron, 2013). LOD variation established rotational jerks,  
 417 particularly of an approximately 6-year variation, which correlate well with  
 418 6 year variations in magnetic signals (Gillet et al., 2010; Chulliat and Maus,  
 419 2014). However, the 2003.5 signal is not linked with the 6 year variation; this  
 420 is not surprising given its appearance in the long-term secular variation in  
 421  $dY/dt$  at the Chinese observatories. There may be two kinds of jerks, one as-  
 422 sociated with the 6-year oscillation, and one, such as the one presented here,  
 423 of different origin, relating to longer term changes in the secular variation,  
 424 shown particularly clearly by the  $dY/dt$  of the Chinese data. Demetrescu

425 and Dobrica (2014) pointed out that jerk arises from the combination of the  
426 internal 22yr and 80 yr signals accoring the decomposition of the geomag-  
427 netic SV.

428 Perturbing the CHAOS-6 model to better fit the new data does not show  
429 evidence of missing structure in the model; large features in the data remain  
430 unfit. As they cannot be explained by a potential field of internal origin, they  
431 probably do not reflect the underlying secular variation. Our results therefore  
432 imply that CHAOS-6 model fits the reliable features in rapid field variation.  
433 To go further, careful treatment of the data, probably requiring analysis of  
434 very noisy monthly mean first differences (rather than annual differences as  
435 here) will be necessary to further constrain the origin of geomagnetic jerks.  
436 However, the new availability (and hopefully extension) of the Chinese data  
437 will provide a powerful tool for further study of this issue.

## 438 **Abbreviations**

439 SV: secular variation; SA: secular acceleration; CMB: core-mantle bound-  
440 ary; LOD: length of day.

## 441 **Author's contributions**

442 YF and RH initiated the study, designed the numerical experiments and  
443 wrote the manuscript. YJ provided the related calculating results, GAC sup-  
444 plied some beneficial suggestions. YF finalized the manuscript. All authors  
445 read and approved the final manuscript.

## 446 **Acknowledgements**

447 The authors would like to thank the support of scientists working at the  
448 Chinese Earthquake Administration for compiling the data in a database.  
449 This work was funded by the State Key Laboratory of Space Weather, Chi-  
450 nese Academy of Sciences, National Natural Science Foundation of China  
451 (Grant No. 41404053) and Jiangsu Government Scholarship for Overseas  
452 Studies. RH and GAC were supported by NERC grant NE/M012190/1.

## 453 **Competing interests**

454 The authors declare that they have no competing interests. This study  
455 does not involve humans/animals.

## 456 **Appendix**

457 The brief description of the treatment to the observatory records. Ob-  
458 servatory data are either presented in a geographic ( $X, Y, Z$ ) or geomagnetic  
459 ( $D, H, Z$ ) coordinate system.

460 BJI-No records for 2007, 2015 and 2016, to get rid of the questionable  $D$  in  
461 2002.

462 CDP-No records for 1997, Baseline correction to  $Z$  in 2003, to reduce the  
463 misfit by subtracting the difference.

464 CHL-No records for 2011, Baseline correction to  $D, H$  and  $Z$  in 2008, to  
465 reduce the misfit by subtracting the difference.

466 CNH-Baseline correction to  $D$  and  $H$  in 2007 and 2008, to reduce the misfit  
467 by subtracting the difference.

468 COM-Baseline correction to  $D$  in the first month in 2000, to reduce the misfit

469 by subtracting the difference.  
 470 COQ-No records before 1998 and period 2011—2014, location had been  
 471 changed since 2014.  
 472 DED-No records for 2006, 2007, 2014 and 2015.  
 473 DLG-No records for 1998, Baseline correction to  $D$ ,  $H$  and  $Z$  in 2000 and  
 474 2001, to reduce the misfit by subtracting the difference.  
 475 ESH-Only has records for 2008—2016.  
 476 GLM-Baseline correction to component  $H$  in 2008, to get rid of 1 day's ques-  
 477 tionable data.  
 478 GYX-No records for 2006, 2006 and 2013 onwards.  
 479 GZH-No records for 1996—2001.  
 480 HHH-No records for 2001, 2002, 2004, 2006 and 2007, baseline correction to  
 481  $D$  in 2003, to reduce the misfit by subtracting the difference.  
 482 HZC-No records for the March, 2007.  
 483 JIH-No records for 2001. Baseline correction to  $D$  and  $H$  in 1996 and 2000,  
 484 to reduce the misfit by subtracting the difference.  
 485 JYG-No records for 1995—1997.  
 486 KSH-Baseline correction to three components in 2000, 2002 and 2006, to re-  
 487 duce the misfit by subtracting the difference.  
 488 LSA-No records for 1995.  
 489 LYH-No records for 1996—1998.  
 490 LZH-No records for 1996, 2007 and 2009.  
 491 MCH-No records for 1997, 2005—2007.  
 492 MCH-Only has records for 2009—2016.  
 493 MZL-No records for 2006.

494 NAJ-No records for 1998, 2002 and 2006 onwards.  
 495 QGZ-No records for 2005 and part of 2012, 2015.  
 496 QIM-Only has records for 2013—2016.  
 497 QIX-No records for part of 2007, baseline correction to  $D$  in 2015 and 2016,  
 498 to reduce the misfit by subtracting the difference.  
 499 QZH-No records for 1999, 2002—2006.  
 500 SQH-Only has records for 2009—2014.  
 501 SSH-No records for 2006—2011.  
 502 SYG-No records for 1997, 2004—2007.  
 503 TAA-No records for 1995, 1996, 1998 and 2003.  
 504 TAY-No records for 1996 and 1997, to get rid of the questionable  $D$  in 2005.  
 505 THJ- Complete records.  
 506 TSY-Baseline correction to  $H$  in 2000, to reduce the misfit by subtracting  
 507 the difference.  
 508 WHN-No records for 1995, and 2007.  
 509 WJH-Only has records for 2013—2016.  
 510 WMQ- No records for 1999, Baseline correction to  $H$  in 2000, to reduce the  
 511 misfit by subtracting the difference.  
 512 XIC- No records for 1997, Baseline correction to  $H$  in 2007, to reduce the  
 513 misfit by subtracting the difference.  
 514 YCB- No records for 1999 and 2000.  
 515 YON- No records for 1995.

516

517 Alexandrescu, F., Gibert, D., Le Mouël, L., Saracco, G., 1996. Worldwide



518 wavelet analysis of geomagnetic jerks. *J. Geophys. Res.: Solid Earth* 101,  
519 21975–21994.

520 Alldredge, L., 1984. A discussion of impulses and jerks in the geomagnetic  
521 field. *J. Geophys. Res.* 89, 128–142.

522 Bloxham, J., Jackson, A., 1992. Time-dependent mapping of the magnetic  
523 field at the core-mantle boundary. *J. Geophys. Res.* 97, 19537–19563.

524 Bloxham, J., Zatman, S., Dumberry, M., 2002. The origin of geomagnetic  
525 jerks. *Nature* 420, 65–68.

526 Brown, W., Beggan, C., Macmillan, S., 2016. Geomagnetic jerks in the swarm  
527 era. In: *Spacebooks. ESA Living Planet Symposium, Czech, Prague*, pp.  
528 9–13.

529 Brown, W. J., Mound, J. E., Livermore, P. W., 2013. Jerks abound: An  
530 analysis of geomagnetic observatory data from 1957 to 2008. *Phys. Earth  
531 Planet. Inter.* 223, 62–76.

532 Chulliat, A., Maus, S., 2014. Geomagnetic secular acceleration, jerks, and a  
533 localized standing wave at the core surface from 2000 to 2010. *J. Geophys.  
534 Res.* 119, 1531–1543.

535 Chulliat, A., Telali, K., 2007. World monthly means database project. *Publs.  
536 Inst. Geophys. Pol. Acad. Sc. C-99 (398)*, 268–274.

537 Courtillot, V., J, D., Le Mouél, J. L., 1978. Sur une accélération récente de la  
538 variation séculaire du champ magnétique terrestre. *C. R. Acad. Sci. Paris.  
539 Ser. D* 287, 1095–1098.

540 Demetrescu, C., Dobrica, V., 2014. Multi-decadal ingredients of the secu-  
541 lar variation of the geomagnetic field. Insights from long time series of  
542 observatory data. *Physics of the Earth and Planetary Interiors* 231, 39–55.

543 Finlay, C., Olsen, N., Kotsiaros, S., Gillet, N., Tøffner-Clausen, L., 2016.  
544 Recent geomagnetic secular variation from Swarm and ground observato-  
545 ries as estimated in the CHAOS-6 geomagnetic field model. *Earth, Planets*  
546 *Space* 68, 1–18.

547 Gillet, N., Jault, D., Canet, E., Fournier, A., 2010. Fast torsional waves and  
548 strong magnetic field within the earth’s core. *Nature* 465, 74–77.

549 Holme, R., De Viron, O., 2013. Characterization and implications of in-  
550 tradecadal variations in length of day. *Nature* 499, 202–204.

551 Holme, R., Olsen, N., Bairstow, F., 2011. Mapping geomagnetic secular vari-  
552 ation at the core-mantle boundary. *Geophys. J. Int.* 186, 521–528.

553 Lodge, A., Holme, R., 2009. Towards a new approach to archaeomagnetic  
554 dating in europe using geomagnetic field modelling. *Archaeometry* 51, 309–  
555 322.

556 Malin, S. R. C., Hodder, B. M., 1982. Was the 1970 geomagnetic jerk of  
557 internal or external origin? *Nature* 296, 726–728.

558 Manda, M., Bellanger, E., Le Mouél, J. L., 2000. A geomagnetic jerk for  
559 the end of the 20th century? *Earth Planet. Sci. Lett.* 183, 369–373.

560 Manda, M., Holme, R., Pais, A., Pinheiro, K., Jackson, A., Verbanac, G.,

561 2010. Geomagnetic jerks: Rapid core field variations and core dynamics.  
 562 Space Sci. Rev. 155, 147–175.

563 Mandeau, M., Olsen, N., 2006. A new approach to directly determine the  
 564 secular variation from magnetic satellite observations. Geophys. Res. Lett.  
 565 33, 147–175.

566 McLeod, M., 1996. Spatial and temporal power spectra of the geomagnetic  
 567 field. J. Geophys. Res. 101, 2745–2763.

568 Mound, J., Buffett, B., 2003. Interannual oscillations in length of day: Im-  
 569 plications for the structure of the mantle and core. J. Geophys. Res. 108,  
 570 253.

571 Mursula, K., Holappa, L., Karinen, A., 2008. Correct normalization of the  
 572 Dst index. Astrophysics and Space Sciences Transactions 4, 41–45.

573 Olsen, N., Mandeau, M., 2007. Investigation of a secular variation impulse  
 574 using satellite data: The 2003 geomagnetic jerk. Earth Planet. Sci. Lett.  
 575 255, 94–105.

576 Pinheiro, K. J., Jackson, A., Finlay, C. C., 2011. Measurements and uncer-  
 577 tainties of the occurrence time of the 1969, 1978, 1991, and 1999 geomag-  
 578 netic jerks. Geochem. Geophys. Geosyst. 12.

579 Sabaka, T. J., Olsen, N., Purucker, M. E., 2004. Extending comprehensive  
 580 models of the earth's magnetic field with ørsted and CHAMP data. Geo-  
 581 phys. J. Int. 159, 521–547.

- 582 Torta, J. M., Pavón-Carrasco, F. J., Marsal, S., Finlay, C. C., 2015. Evidence  
583 for a new geomagnetic jerk in 2014. *Geophys. Res. Lett.* 42, 7933–7940.
- 584 Wardinski, I., Holme, R., 2006. A time-dependent model of the Earth’s mag-  
585 netic field and its secular variation for the period 1980-2000. *J. Geophys.*  
586 *Res.: Solid Earth* 111, 1–14.
- 587 Wardinski, I., Holme, R., 2011. Signal from noise in geomagnetic field mod-  
588 elling: Denoising data for secular variation studies. *Geophys. J. Int.* 185,  
589 653–662.

Figure 1: Locations of 43 Chinese observatories. (red squares: 10 principally investigated observatories –THJ, JIH, QIX, GLM, TSY, COM, YON, WMQ, DLG and CHL). Lambert Conformal Projection.

Figure 2: Locations of 7 European observatories (BEL, CLF, DOU, FUR, HLP, HRB and NGK). Lambert Conformal Projection.

Figure 3: Comparison of uncorrected annual differences of monthly means of  $X$ ,  $dX/dt$ , between China (top) and Europe (bottom). Vertical black dash lines correspond to possible jerk times in 2003.5 and 2014.

Figure 4: Comparison of uncorrected annual differences of monthly means of  $Y$ ,  $dY/dt$ , between China (top) and Europe (bottom).



Figure 5: Comparison of uncorrected annual differences of monthly means of  $Z$ ,  $dZ/dt$ , between China (top) and Europe (bottom). The Chinese  $dZ/dt$  data are additionally linearly detrended (middle).

Figure 6: Eigenvalues of components  $dX/dt$ ,  $dY/dt$  and  $dZ/dt$  of 10 Chinese (red line) and 7 European (black line) observatories.

Figure 7: The components of the eigenvectors corresponding to the largest eigenvalue for the 10 Chinese observatories. Squares:  $dX/dt$ ; diamonds:  $dY/dt$ ; stars:  $dZ/dt$ .

Figure 8: Normalization of the largest eigenvalue eigenvector for all 43 Chinese observatories, on full (left) and expanded (right) axes. Red squares: good observatories; black circles: less good observatories.

Figure 9: The comparison between the noisy contributions from China and Europe with annual differences of monthly means of Dcx index. Black line: Noisy contributions from China; blue line: Noisy contributions from Europe; red line: Annual differences of Dcx.

Figure 10: Comparison of denoised annual differences of monthly means of  $X$ ,  $dX/dt$ , between 10 Chinese and 7 European observatories.

Figure 11: Comparison of denoised annual differences of monthly means of  $Y$ ,  $dY/dt$ , between 10 Chinese and 7 European observatories.

Figure 12: Comparison of denoised annual differences of monthly means of  $Z$ ,  $dZ/dt$ , between 10 Chinese and 7 European observatories.



Figure 13: Denoised annual differences of monthly means of  $Y$ ,  $dY/dt$ , of 10 Chinese observatories.

Figure 14: Denoised annual differences of monthly means of  $Z$ ,  $dZ/dt$ , of 7 European observatories.

Figure 15: The variation of  $dY/dt$  of GLM.

Figure 16: The variation of  $dX/dt$  of YON under different damping parameters.

Figure 17: The variation of  $dY/dt$  of YON under different damping parameters.

Figure 18: The variation of  $dZ/dt$  of YON under different damping parameters.